

Homework 2
Due by Midnight on 10/02/2015

Instructions:

- (1) All parts must be completed for credit
 - (2) You must show work to receive credit
 - (3) You must turn in homework on Canvas!
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Question 1: Properties of Probability (20pts)

Each day on Boston College campus, 60% of all students read a source of current events (e.g. newspaper), while 80% use social media.¹ 50% of students partake in both activities daily. If a student is randomly selected what is the probability that:

- (a) The selected student either reads current events or uses social media?
- (b) That the student takes part in **only one** of the activities?

¹Numbers made up by instructor

Question 2: Properties of Probability (30pts)

Suppose you roll a pair of dice, and take the sum. Let A be the event that you observe an even number. Let B be the event that you observe a number greater than seven. Begin by writing down the two sets A & B as well as the sample space.

(a) What is the intersection of A & B ? What is the complement of \bar{A} ? What is the complement of \bar{B} ?

(a) What is $\bar{A} \cap B$? What is $\bar{A} \cup B$?

(c) What is $\bar{A} \cup \bar{B}$? What is $\bar{A} \cap \bar{B}$?

(d) Are A and B mutually exclusive? Are they collectively exhaustive? If not, write down two sets that would satisfy these definitions.

Question 3: Conditional Probability & Bayes Rule (30pts)

1 in 1000 adults is afflicted with a rare disease for which the a diagnostic test has been developed. A positive result occurs 99% of the time when the individual actually has the disease and 2% of the time when the individual does not have the disease.

- (a) What is the probability that a random person selected has the disease and they receive a positive result?
- (b) What is the probability that, if a random individual tests positive, he actually has the disease?
- (c) Does this result make sense to you?

Question 4: Permutations and Combinations (20pts)

There are ten teaching assistance available for a statistics course at a large state university. Throughout the semester the professor must assign various tasks.

(a) Grading: The professor gives a midterm exam with four questions, and needs to grade the exam. He would like to have a different TA grade each question, and thus assign one assistant to grade each question. How many ways can he choose assistants for grading?

(b) Office hours: Each week four TAs must hold office hours at the 1pm on Thursdays. How many ways may the professor assign TAs to this task?